

Discussion of “Optimal Monetary Policy with Redistribution” by Jennifer La’O and Wendy Morrison

Joao Guerreiro

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Normative HANK literature: how does heterogeneity change optimal monetary policy?

- Distributional considerations are an important concern for monetary policy.
[Bhandari-Evans-Golosov-Sargent (2021), Achary-Challe-Dogra (2020), LeGrand-Martin-Baillon-Ragot (2021), Nuno-Thomas (2019), McKay-Wolf (2022), Smirnov (2022), Davila-Schaab (2023),...]
 - Incomplete markets, heterogeneous productivity, idiosyncratic inc. risk, cyclical income risk, nominal rigidities...
 - Redistribution vs. insurance? Redistribution of financial wealth vs. labor income?

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 - Redistribution vs. insurance? Redistribution of financial wealth vs. labor income?

Here: Focus instead on **ex-ante heterogeneity/types**.

- Complete markets, heterogeneous productivity, **shocks to the income distribution**, nominal rigidities...

Werning (2007) + Correia-Nicolini-Teles (2008)

- But, also assume **non-contingent linear taxation**.

Great paper!!!

- **Monetary policy with redistribution:** Focus on ex-ante heterogeneity.

Generally **optimal** to **deviate** from **price stability**.

- High markup in high inequality states.
- Result rooted on failure of Diamond-Mirrlees theorem.
 - Incomplete set of tax instruments – tax rates are non-contingent.

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This discussion focuses on:

1. Assumptions on available tax instruments are crucial.
2. Implications of progressive versus linear taxation.

A (very) simplified model: static and aggregate shock $s \in \{1, 2, \dots, S\}$

$$\text{Households: } \max \sum \mu_s \left[u(c_{i,s}) - v\left(\frac{\ell_{i,s}}{\theta_{i,s}}\right) \right] \quad \text{s.to} \quad \sum_s q_s \{c_{i,s} - (1 - \tau_s^n) w_s \ell_{i,s} - T_s\} = 0$$

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Firms:

[Monopoly distortion corrected]

- Flexible price: $p_s^{\text{flex}} = P_s w_s$
- Sticky price: $p_s^{\text{stick}} = \varepsilon_s P_s w_s = \mathbb{E}[\Theta_s P_s w_s]$
- Using agg price definition

$$w_s = w(\varepsilon_s) = \frac{1}{\mathcal{M}(\varepsilon_s)}$$

[Here: Real wage = inverse markup]

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Monetary policy: $M_s = P_s C_s$

Resource constraint: $C_s = \Delta(\varepsilon_s) L_s$

- $\Delta(\varepsilon_s) \leq 1$, maximized at $\varepsilon_s = 1$ and concave.

Equilibrium and implementability conditions

Equilibrium equations:

$$\frac{\mu_s u'(c_{i,s})}{\mu_1 u'(c_{i,1})} = \frac{q_s}{q_1},$$

$$\sum_s q_s \{c_{i,s} - (1 - \tau_s^n) w(\varepsilon_s) \ell_{i,s} - T_s\} = 0$$

$$\frac{v' \left(\frac{\ell_{i,s}}{\theta_{i,s}} \right) \frac{1}{\theta_{i,s}}}{u'(c_{i,s})} = (1 - \tau_s^n) w(\varepsilon_s)$$

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Reduce the number of implementability conditions:

1. Must require $\mu_s u'(c_{i,s}) / \mu_1 u'(c_{i,1})$ be constant across i .
 - Utility with constant elasticity: $c_{i,s} = \omega_i^s C_s$

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2. Only one labor tax, so $v' \left(\frac{\ell_{i,s}}{\theta_{i,s}} \right) \frac{1}{\theta_{i,s}} / u'(c_{i,s})$ is constant across i .

- Utility with constant elasticities: $\ell_{i,s} = \omega_{i,s}^l L_s$, where $\omega_{i,s} = (\omega_i^c)^{-\frac{\gamma}{\eta}} \theta_{i,s}^{\frac{1+\eta}{\eta}} / \sum_i \pi_i (\omega_i^c)^{-\frac{\gamma}{\eta}} \theta_{i,s}^{\frac{1+\eta}{\eta}}$

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3. Resource constraints and the following constraints:

$$\sum_s \mu_s \left\{ u'(c_{i,s}) c_{i,s} - v' \left(\frac{\ell_{i,s}}{\theta_{i,s}} \right) \frac{\ell_{i,s}}{\theta_{i,s}} \right\} = \bar{T}$$

Ramsey optimum

The problem is: $\max_{\{\sum_i \pi_i \omega_i^c = 1\}} \sum_i \lambda_i \sum_s \mu_s \left[u(\omega_i^c C_s) - v\left(\frac{\omega_{i,s}^l L_s}{\theta_{i,s}}\right) \right]$ subject to

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1. $\Delta'(\varepsilon_s) = 0 \Leftrightarrow \varepsilon_s = 1$.

- **Price stability** is optimal $P_s = P$.

[Diamond-Mirrlees (1971) prod. efficiency]

[Correia-Nicolini-Teles (2008)]

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[Diamond-Mirrlees (1971) prod. efficiency]

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2. Optimal labor tax:

$$1 - \tau_s^n = \frac{\sum_i \eta_i^c \{\lambda_i + \varphi_i (1 - \gamma)\}}{\sum_i \eta_{i,s}^\ell \{\lambda_i + \varphi_i (1 + \eta)\}}, \quad \eta_{i,s}^\ell \equiv \frac{\eta_i^c}{\omega_i^c} \left(\frac{\theta_{i,s}^{\frac{1+\eta}{\eta}} \alpha_i^{-\frac{\gamma}{\eta}}}{\sum_j \pi_j \alpha_j^{-\frac{\gamma}{\eta}} \theta_{j,s}^{\frac{1+\eta}{\eta}}} \right).$$

- Generally, failure of uniform labor taxation across states (despite constant elasticities).

[Werning (2007)]

- Ex-ante average tax rate on individual i :

$$\bar{\tau}_i^n \equiv \frac{\sum_s q_s w_s \ell_{i,s} \tau_s^n}{\sum_s q_s w_s \ell_{i,s}} = \frac{\sum_s \frac{q_s w_s L_s}{\sum_s q_s w_s L_s} \omega_{i,s}^\ell \tau_s^n}{\sum_s \frac{q_s w_s L_s}{\sum_s q_s w_s L_s} \omega_{i,s}^\ell} = \bar{\tau}^n + \text{COV}_i \left(\tau_s^n, \frac{\omega_{i,s}^\ell}{\omega_i^\ell} \right)$$

So, why deviate from price stability?

Paper: Crucially, assume non-contingent taxes $\tau_s^n = \tau^n$. Additional constraint:

$$\frac{v' \left(\frac{\ell_{i,s}}{\theta_{i,s}} \right) \frac{1}{\theta_{i,s}}}{u' (c_{i,s})} \frac{1}{w(\varepsilon_s)} = \frac{v' \left(\frac{\ell_{i,1}}{\theta_{i,1}} \right) \frac{1}{\theta_{i,1}}}{u' (c_{i,1})} \frac{1}{w(\varepsilon_1)}$$

Proportional income shocks: uniform labor taxation is optimal \Rightarrow constraint does not bind.

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Shocks to (log-)inc. dispersion: Target **state-contingent markup**.

- **Approx. state-contingent** taxes using ε_s to impose wedge between wage and productivity.
 - How? **Price instability**. So, Diamond-Mirrlees (1971) fails...
- Is it optimal to fully replicate previous? No, because of Tack Yun distortion: $C_s = \Delta(\varepsilon_s) L_s$.
- **Low real wage** (high markup) in states with **high inequality**.

Which instruments and how?

Avail. Inst.	Labor taxes	Monetary policy	Note
1. $T_{i,s}, \tau_{i,s}^n$	$\tau_{i,s}^n = 0$	Price stability	All redistribution with $T_{i,s}$

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4. T_s, τ_s^n	$1 - \tau_s^n = \frac{\sum_i \eta_i^c \{\lambda_i + \varphi_i(1-\gamma)\}}{\sum_i \eta_{i,s}^\ell \{\lambda_i + \varphi_i(1+\eta)\}}$	Price stability	$\tau_s^n \uparrow$ in high inequality states Approx 3.: $\bar{\tau}_i^n = \bar{\tau}^n + \text{COV}_i \left(\tau_s^n, \frac{\omega_{i,s}^\ell}{\bar{a}_i^\ell} \right)$ Prop. shocks: $\bar{\tau}_i^n = \bar{\tau}^n$ always!

Proportional shocks: cannot change ex-ante avg. tax rates.

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5. T_s, τ^n	...	State-cont. markup	$\mathcal{M}(\varepsilon_s) \uparrow$ with \uparrow inequality states Unless proportional shocks Approximate 4.

Progressive taxation

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- Natural to consider **progressive income taxation**... Suppose following tax code:

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Simple changes to the Ramsey problem:

$$\max \sum_i \lambda_i \sum_s \mu_s \left[u(\omega_i^c C_s) - v\left(\frac{\omega_{i,s}^l L_s}{\theta_{i,s}}\right) \right]$$

subject to

$$\sum_s \mu_s \left\{ u'(\omega_i^c C_s) \omega_i^c C_s - \frac{1}{1-p} v'\left(\frac{\omega_{i,s}^l L_s}{\theta_{i,s}}\right) \frac{\omega_{i,s}^l L_s}{\theta_{i,s}} \right\} = \bar{T}, \quad C_s = \Delta(\varepsilon_s) L_s$$

where $\omega_{i,s}^l$ is also affected by p ...

Price stability still optimal. Optimal tax level:

$$1 - \tau_s = \frac{\sum_i \eta_i^c \{ \lambda_i + \varphi_i (1 - \gamma) \}}{\sum_i \eta_{i,s}^\ell \left\{ \lambda_i + \varphi_i \frac{1+\eta}{1-p} \right\}} L_s^p, \quad \eta_{i,s}^\ell \equiv \frac{\eta_i^c}{\omega_i^c} \left(\frac{\theta_{i,s}^{\frac{1+\eta}{\eta+p}} (\omega_i^c)^{-\frac{\gamma}{\eta+p}}}{\sum_j \pi_j (\omega_j^c)^{-\frac{\gamma}{\eta+p}} \theta_{j,s}^{\frac{1+\eta}{\eta+p}}} \right)^{1-p}$$

1. Progressivity ($p > 0$): decreases the concern with shocks to $\theta_{i,s}$.
2. **New**: $1 - \tau_s$ also depends on aggregate labor L_s .
 - Lower taxes ($\tau_s \downarrow$) in states with high labor L_s .

⇒ Proportional income shocks are no longer sufficient for $\tau_s = \tau$!

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Q1: Optimal monetary policy when τ_s is constrained?

Q2: What if we allow even more freedom in designing labor income taxes?

Great paper!!!

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Generally **optimal** to **deviate** from **price stability**.

- High markup (low real wage) in high inequality states.
- Result rooted on failure of Diamond-Mirrlees theorem.
 - Incomplete set of tax instruments – tax rates are non-contingent.
 - Also, failure of uniform labor taxation due to shocks to relative productivities.

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1. Assumptions on available tax instruments are crucial.
2. Implications of progressive versus linear taxation.